$b^2 \quad xy = ab^2$ $xy = ab^2 \quad g(x)$ a°= $A\hat{C}B=\frac{2}{5}A\hat{B}D$ a^2 В 0= P X = 1 0 2C 2C 0 2× ABCD $\frac{P}{1+\frac{P}{1200}} + \frac{P}{100} = 0$ 1. 211 M

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